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4 **Multi-Objective Traffic Network Design Accounting for Plug-in Electric Vehicle Energy**  
5 **Consumption**  
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*Abstract*

In order to exploit the potential of plug-in electric vehicles (PEVs) as a sustainable form of transport, this novel technology must be integrated into the traditional transport system planning process. This work takes a step in that direction by incorporating PEV energy consumption rates into network design decisions. Not only is energy consumption a proxy for emissions in traditional vehicles, it will also become an essential issue for regional energy providers who will need to adapt to the additional electricity demand created as PEVs become a more ubiquitous form of transport. This work addresses the network design problem (NDP) to minimize both system level energy consumption and total system travel time, independently and as a multi-objective problem. The NDP is formulated and solved for a road network with a high penetration of PEVs using a heuristic approach. For certain design scenarios, minimizing total system travel time and minimizing energy consumption are demonstrated to be conflicting objectives. The tradeoff in terms of each system performance measure is quantified. Based on the results it is evident that both objectives must be considered when planning for future networks that will be comprised of some portion of PEVs.

## 49 1. INTRODUCTION

50 Electric vehicles are experiencing a surge in popularity due to advancements in technology,  
51 their potential to reduce harmful emissions originating from traditional petroleum-fuelled  
52 vehicles, and a greater emphasis on global sustainability in many sectors. While the  
53 beneficial environmental impact provides ample motivation for investigation, it is also  
54 important to note that PEVs introduce a closer tie between the road network and the electric  
55 power system that will require new collaborations and modeling tools to effectively exploit.  
56 Traditionally electric power systems operators have needed to predict energy demand that  
57 results from static sources (e.g., households, buildings, industries). However, when PEVs  
58 achieve a small but significant level of market penetration, the aggregate mobile energy use  
59 generated by users' driving patterns will comprise a substantial new form of energy demand.  
60 Predicting this new source of energy demand requires a model based on a cross-disciplinary  
61 platform that captures vehicle driving patterns, PEV energy use, PEV market locations, and  
62 spatiotemporal charging behavior.

63 The transport problem of interest in this work is the well-known network design  
64 problem (NDP), which identifies the capacity enhancements for a network to achieve a stated  
65 objective. The traditional NDP objective is minimizing total system travel time (TSTT). In  
66 this work an additional objective is considered – minimizing total system energy  
67 consumption (TSEC) – where the energy is generated by PEV mobile activity in a network.  
68 Both single and multi-objective NDPs are evaluated. The sub-problem of the road network  
69 design problem is user equilibrium (UE) assignment. As part of the UE sub-problem the  
70 proposed model tracks the two classes of vehicles (PEVs and traditional internal combustion  
71 engine vehicles (ICEVs)) through the network in order to quantify their energy consumption.  
72 The energy consumption of vehicles is calculated using a speed-variable model that is  
73 established on real data from reputable sources in industry. Based on the UE vehicular  
74 trajectories and calculated energy consumption rates, this work implements a heuristic  
75 method, a genetic algorithm, to solve the various network design problems. The tradeoff  
76 between TSTT and TSEC is compared under different design objectives and different budget  
77 constraints.

78 Hence, the motivation for this work is twofold: to explore the effects of an additional  
79 performance measure (energy consumption by PEVs) on network design decisions and to  
80 advance research that will aid the potential convergence of the transportation road network  
81 and the electric power system. Furthermore, dozens of cities around the world are conducting  
82 projects to evaluate the potential of PEVs in their region (1), (2). An essential component of  
83 such a forecast is tied to the energy consumption which directly leads to additional demand  
84 on the electric grid at the household, neighborhood, and regional levels. Given the novelty of  
85 PEV technology, these forecasts are generally based on annual vehicle travel estimates and  
86 static energy consumption estimates, or estimated battery capacities. This work addresses the  
87 issue of additional demand, and provides a more accurate estimation by exploiting each  
88 driver's disaggregate travel patterns as revealed by the UE assignment model, computing the  
89 respective energy consumption, and aggregating across vehicles in the network. This type of  
90 analysis is integral for power systems tasked with predicting regional demands. In many  
91 situations, energy consumption can be used as a proxy for emissions production and thus a  
92 network that minimizes energy consumption will also be environmentally beneficial.

93 This work begins with a short literature review focusing on the NDP in Section 2,  
94 while Section 3 introduces the mathematical model for the problem. Section 4 discusses the  
95 solution methodologies employed in this research, Section 5 presents the computational  
96 results, and Section 6 concludes this work with remarks about future directions for research.

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## 99 2. LITERATURE REVIEW

100 This work focuses on the NDP with added element of tracking the energy consumption of  
101 vehicles through the network. Formulations and solution algorithms for the traditional traffic  
102 network design problem exist in many variations and applications; however, to the authors'  
103 knowledge this is the first work that examines the energy consumption of PEVs. Most  
104 generally, network design is conceptually simple: the problem of finding the optimal  
105 location(s) to enhance a network given limited "budget." Such enhancements are generally  
106 capacity improvements that can have a variety of interpretations, from the discrete additions  
107 (e.g., lanes, roads) to project that may have a more continuous nature (e.g., optimized signal  
108 timing plans, other projects like widening of shoulders, etc.). The NDP is traditionally  
109 formulated as a bi-level mathematical programming problem, where the upper level  
110 represents the "planner's" perspective that measures the impact in the network due to the  
111 change, and the lower level represents the users' reaction to those changes (3).

112 Early work on the NDP concentrated on formulating the problem to approximate  
113 planning applications and developing efficient algorithms to solve these formulations.  
114 Leblanc pioneered the use of the branch and bound method to solve the single-objective  
115 discrete NDP (4). A convex, system-optimal formulation was introduced by Danzig et al and  
116 solved using a decomposition algorithm (5). Chen and Alfa also attempted the discrete NDP,  
117 in which they minimized travel cost and combined trip assignment and distribution (6). Chen  
118 and Alfa proposed a discrete stochastic UE NDP using an incremental traffic assignment  
119 approach (7). Davis later solved this formulation using a heuristic algorithm (8). While a few  
120 works have been highlighted here, a more comprehensive evaluation can be found in (9) or  
121 (2).

122 Some of the more recent work in the field is concerned with more complex multi-  
123 objective formulations and applications. The multi-objective network design problem  
124 (MNDP) uses a weighted combination of different objectives. This is a more realistic  
125 approach to modeling a complex transport system, but it also results in a more difficult  
126 mathematical problem to solve. Friesz et al first proposed a multi-objective network design  
127 and solved it through a simulated annealing inspired heuristic (10), which was extended by  
128 (11). Additionally, heuristic solution methods have been used by other researchers to solve  
129 the bi-level traffic NDP for a number of applications including multi-objective signal timing  
130 (12), accounting for demand uncertainty (13), optimal toll pricing strategies (14), examining  
131 the impact of environmental justice considerations (15), and minimizing emissions (16-17).

132 While the authors are unaware of previous works attempting to combine the NDP and  
133 PEVs, researchers have begun to incorporate the impact of PEVs into other traditional  
134 transport models. Artmeier et al introduced a vehicle routing problem where PEVs can use  
135 regenerative braking to regain battery power and extend their range (18). Jiang et al also  
136 formulated a constrained shortest path problem, and apply it in a traffic assignment model  
137 that is solved using a Frank-Wolfe based algorithm (19). Most notably, (20) introduced a  
138 model that tracks vehicle energy consumption, similar to the one employed in the lower level  
139 problem in this work. However, the previous work is concerned with the impact of travel  
140 demand variability on PEV energy consumption, while this one uses a heuristic approach to  
141 solve the discrete NDP and examines the tradeoffs between minimizing for different  
142 objectives.

## 143 3. MATHEMATICAL MODEL

144 The formal mathematical formulation of the NDP, UE assignment model, and system  
145 performance measures are presented in this section. Consider a transportation network  $G =$   
146  $(N, A, \mathbf{D}, \mathbf{W}, \mathbf{T})$  consisting of a set of nodes  $N$ ; a set of directed arcs  $A$ ; a demand matrix  $\mathbf{D}$   
147 with  $|N|$  rows and columns, mapping the demand for travel from every node to every other  
148

149 node; the  $|N| \times |N|$  matrix  $\mathbf{W}$  representing the percentage of each origin-destination demand  
 150 consisting of PEVs; and  $\mathbf{T}$ , a vector of link cost functions for all links in the network.

151 The multi-objective network design problem is formulated as a bi-level problem. The  
 152 upper level seeks to minimize total system energy consumption,  $E$ , or total system travel  
 153 time,  $Z$ , by adding the capacity on some number of links subjected to a total budgetary  
 154 constraint. The lower level problem is the user equilibrium model with PEVs that will be  
 155 further discussed in Section 4.2. Users react to the capacity changes that are implemented by  
 156 the system operators in the ‘‘upper level’’, which lends itself to the bi-level formulation. The  
 157 formulation for the upper level problem is shown below for the objective of energy  
 158 minimization (the same formulation holds for the objective of minimizing TSTT, with  $E$   
 159 replaced by  $Z$  in the objective function):

$$\text{Minimize } E \quad (1)$$

s.t.

$$E = \sum_{a \in A} [EC_{ICEV}(s_a)v_a^{ICEV} + EC_{PEV}(s_a)v_a^{PEV}] \quad (2)$$

$$Z = \sum_a v_a t_a(v_a, \delta_a) \quad (3)$$

$$\sum_{\forall a} g_a(\delta_a) \leq B \quad (4)$$

$$\delta_a \geq 0 \quad \forall a \in A \quad (5)$$

160 Where  $\delta_a$  is the capacity added to link  $a$ ,  $g_a(\delta_a)$  is the function that represents the cost of  
 161 adding that amount of capacity to link  $a$ , and  $B$  is the total budgetary constraint. The lower  
 162 level problem outputs the ICEV and PEV link level flows,  $v_a^{ICEV}$  and  $v_a^{PEV}$  respectively, and  
 163 link travel times  $t_a$  (and thus link average speed,  $s_a$ ). Therefore  $Z$  represents the total system  
 164 travel time, and  $E$  represents total system energy consumption, computed by summing the  
 165 energy consumption for all vehicles on a link, for all links in the network, based on the speed-  
 166 variable equation that will be presented in Table I.

167 The lower level problem represents the users’ reaction to the network changes. The  
 168 formulation of this model requires some additional notation: the demand matrix  $\mathbf{D}$  represents  
 169 the aggregate demand for both ICEVs and PEVs. Let  $R$  and  $S$  represent the set of all origins  
 170 and destinations respectively, while  $r \in R$  and  $s \in S$  are indexes representing one particular  
 171 origin and destination respectively and  $d_{rs}$  denotes the demand between origin  $r \in R$  and  
 172 destination  $s \in S$ . The percentage of each origin-destination demand realization that are  
 173 PEVs is  $z_{rs}$ , ( $0 \leq z_{rs} \leq 1$ ), which is specified a priori. Let  $k \in K_{rs}$  represent the set of paths  
 174 connecting origin  $r \in R$  and destination  $s \in S$ ,  $f_k^{rs}$  represent the total (ICEV and PEV) flow  
 175 on path  $k$  connecting origin  $r$  and destination  $s$ , and  $\delta_{ak}^{rs}$  be the link path incidence variable.  
 176 The mathematical programming formulation for the lower level problem is then (based on  
 177 (21)):

$$\text{Minimize } \sum_{\forall a} \int_0^{v_a} t_a(y) dy \quad (6)$$

s.t.

$$\sum_k f_k^{rs} = z_{rs}d_{rs} + (1 - z_{rs})d_{rs} \quad \forall r \in R, \forall s \in S \quad (7)$$

$$f_k^{rs}, v_a \geq 0 \quad \forall k \in K_{rs}, \forall r \in R, \forall s \in S \quad (8)$$

$$v_a = \sum_r \sum_s \sum_k f_k^{rs} \delta_{ak}^{rs} \quad \forall a \in A \quad (9)$$

$$v_a^{ICEV} + v_a^{PEV} = v_a \quad \forall a \in A \quad (10)$$

178 The link cost function may be any function that defines the relationship between the  
 179 number of users traveling a particular link and the cost to travel that particular link (e.g.,  
 180 travel time, money, emissions, etc). The Bureau of Public Records (BPR) function is a  
 181 common choice in both transportation literature and in practice, and was used in this work:

$$t = t_0 \left( 1 + \alpha \left( \frac{v}{C + \delta} \right)^\beta \right) \quad (11)$$

182 Where  $t$  is link travel time,  $t_0$  is free-flow travel time (miles per hour),  $v$  is hourly  
 183 volume (vehicles),  $C$  is hourly capacity (vehicles per hour (vph)), and  $\alpha$  and  $\beta$  are parameters  
 184 that depend on link geometry. The UE problem in the lower level was solved used a Frank-  
 185 Wolfe based linearization method. The next section describes the genetic algorithm that was  
 186 used to solve the upper level design problem.

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#### 188 4. SOLUTION METHODOLOGY

189 The following section describes the solution methodology implemented for the above  
 190 problem. Three main components of the methodology are described: the upper level network  
 191 design problem, the lower level user equilibrium assignment problem, and the energy  
 192 consumption model used to compute TSEC.

193

##### 194 4.1 Network Design Problem

195 The network design problem as formulated in the above section cannot be solved to a  
 196 guaranteed global optimal value using known optimization techniques because of the non-  
 197 convex cost function. Therefore heuristic solution methods are necessary. This research  
 198 applied a genetic algorithm (GA), a technique inspired by principles of natural evolution.  
 199 GAs provide a flexible, rigorous, scalable framework to solve challenging optimization  
 200 problems, and are a relatively common research method to solve the bi-level traffic network  
 201 design problem. Additionally, (22) showed that in terms of heuristic approaches to solve the  
 202 continuous NDP, GAs perform better than simulated annealing or random search algorithms.  
 203 Because GAs are a heuristic method, they correctly identify local extrema that are not  
 204 guaranteed to be the global optimal value.

205 A GA locates an optimal solution by searching for promising regions in which there  
 206 are a high proportion of “good” solutions. It begins with a randomly generated initial  
 207 population of individuals that represent potential solutions, and over time, the population  
 208 evolves according to a “natural selection” process, where the best individuals are identified  
 209 and combined using a crossover technique to form new populations of individuals. A basic  
 210 genetic algorithm is outlined below:

- 211 1. Begin by randomly generating a population of  $n$  chromosomes;
- 212 2. Evaluate the fitness  $f(x)$  of each chromosome  $x$  in the population;
- 213 3. Create a new population by iterating the following steps until the new population is  
 214 filled:
  - 215 a. Select two parent chromosomes (with fitter individuals having a higher  
 216 likelihood of being chosen)
  - 217 b. Using a crossover probability, form a new offspring from the two parents;  
 218 without crossover, child will be exact copy of a parent.
  - 219 c. Mutate new offspring using a mutation probability;

- 220           d. Accept and place offspring into new generation of population.  
221       4. Check to see if convergence criteria is met; if yes, stop. Else, return to Step 2 using  
222       the new generation.

223       Both single- and multi-objective variations of the nondominant sorting genetic  
224       algorithm II (NSGA-II) by (23) were used in this work. NSGA-II is a well-known algorithm  
225       that has proven to be the best GA tool for solving multi-objective optimization problems (23).  
226       This algorithm utilizes several techniques that provide superior performance. The feasibility  
227       of solutions is handled by penalizing infeasible individuals in such a way that ensures that  
228       feasible solutions are ranked higher than infeasible solutions, which are ranked higher than  
229       infeasible solutions with greater constraint violations. Additionally, solutions are labeled  
230       according to their efficiency front and the density of surrounding solutions, which makes the  
231       selection process more efficient and preserves the diversity of solutions within a population  
232       (23). See ((12)-(17)) for other examples that utilize NSGA II for various applications of the  
233       traffic network design problem.

234       In this application of a GA, discrete variables were used to represent the additional  
235       capacity on a link, represented in binary form, with one bit allocated to each link such that a  
236       ‘1’ identified the link for improvement and a ‘0’ meant the link would stay the same. Thus an  
237       individual chromosome represented the capacity changes for all links in the network, and a  
238       population carried the different possibilities for discretely adding capacity to some number of  
239       links. During the crossover operation, two new capacities are generated for a link by  
240       combining the first part of the binary capacity representation from one “parent” with the  
241       second part of the binary capacity representation of the other “parent”. An important factor in  
242       the performance of the NSGA II (and all GAs) are the input parameters, which are case  
243       specific to any problem. As such, input settings were determined using sensitivity analysis  
244       and are further discussed for each of the test cases in section 5.

245

#### 246 **4.2 Traffic Assignment Model**

247       The design problem presented here uses the traffic assignment formulation based on the well-  
248       known Wardropian equilibrium for the lower level problem to represent traveler behavior  
249       (24). In this formulation, users will choose a path to minimize their own travel; collectively,  
250       resulting in a state of network equilibrium, where no user can independently change paths for  
251       a shorter travel time. This model is straightforward, flexible, and appropriate for this  
252       application, which employs a heuristic solution method based on iteration in which the UE  
253       model must be computed many times. However, this model is static so it does not capture the  
254       effects of acceleration or gradient (which could be important for PEVs in a regenerative  
255       braking scenario).

256       The UE model distinguishes between two “classes” of vehicles, PEV and internal  
257       combustion engine vehicles (ICEVs). The model assumes that these two vehicles types do not  
258       differ in terms of user behavior; thus, all drivers will make decisions based on minimizing  
259       their travel time, not accounting for potential charging incentives at the destination or range  
260       anxiety, either of which might change route choice decisions from a PEV driver.  
261       Additionally, the model assumes there are no charging opportunities available from public  
262       infrastructure, therefore all vehicles charge at home and begin each trip with a fully charged  
263       battery. PEVs and ICEVs differ based on the former’s limited all-electric range. This model  
264       only applies to the energy consumption of all-electric vehicles, although with a different  
265       energy consumption model, plug-in hybrid electric vehicles could also be represented. The  
266       next section discusses how the traffic assignment model is combined with an energy  
267       consumption model to find the total energy use of PEVs in the traffic network.

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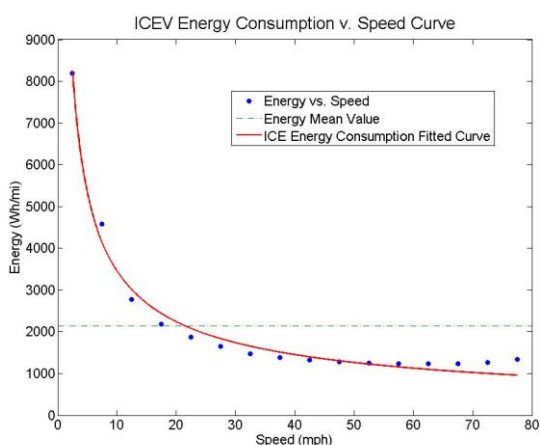
269 **4.3 Energy Consumption Evaluation**

270 The energy consumption of PEVs is a particularly important issue for regional electricity  
 271 providers, who will need to know about the electricity demand created by the use of PEVs. In  
 272 particular, electric power systems managers will be interested in knowing where and when  
 273 PEVs will plug in, how much electricity they will need, and the power management scheme  
 274 that will be utilized (i.e., smart charging). The proposed model takes a first step in answering  
 275 these questions by quantifying *how much* energy will be consumed by the PEVs. A traffic  
 276 assignment model is exploited to answer this question by providing individual user travel  
 277 patterns and average speeds, from which energy consumption can be closely approximated.

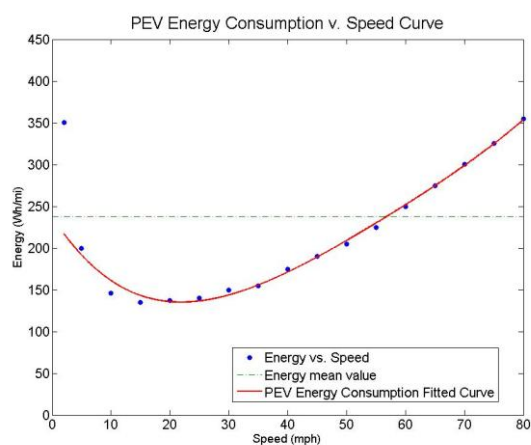
278 However, vehicle energy consumption rates are difficult to quantify, even for ICEVs  
 279 which have a longer history in both practice and research. Existing commercial software  
 280 often uses a dynamic simulation method that was developed based on extensive testing and  
 281 data. However, such a method can be computationally cumbersome, depends on driving  
 282 cycles to predict the mobility of the vehicles (which are not always a representative of real-  
 283 world driving, see (25), and the software itself can be prohibitively expensive.

284 Few empirical results exist for the energy consumption of PEVs (26), although this  
 285 dataset is expanding rapidly. A great deal of research has focused on the long-term impact of  
 286 the energy consumption of PEVs (27), but it is usually based on average driving distances,  
 287 driving cycles, and average per mile estimates. This work is an improvement over past  
 288 models because it is able to capture the speed-varying energy use of vehicle energy  
 289 consumption. Future versions of this model will account for more complex factors such as the  
 290 impact of congestion and gradient effects like acceleration and braking.

291 The energy consumption model for ICEVs in this work was based on data from the  
 292 Environmental Protection Agency’s MOVES 2010a (Motor Vehicle Emissions Simulator)  
 293 software package (28). This software finds energy consumption and emissions production  
 294 from vehicles based on a variety of factors including meteorology, vehicle fleet composition  
 295 (vehicle miles travelled (VMT) estimates, vehicle age distribution, vehicle populations, sales  
 296 and VMT growth rates), vehicle activity, fuel characteristics, and emission control program  
 297 data. The points in Figure 1a show the energy consumption for an average ICEV depending  
 298 on speed obtained (in during the summer AM peak hour in Travis County) from MOVES.  
 299 The curve was fitted to the data using the power regression tool in Matlab. This regression  
 300 model is less accurate at higher speeds, when the efficiency of ICEVs in reality begins to  
 301 decrease. Therefore, for this model to be applied to networks where speeds above 75 mph are  
 302 present, an adjusted energy consumption curve would be necessary.  
 303



(a)



(b)



**FIGURE 1 (a) the energy consumption model for ICEVs based on MOVES2010a and (b) the energy consumption model for PEVs based on data from Tesla.**

Based on the powertrain configuration, PEVs consume energy in a different manner from ICEVs. At lower speeds (like what might result from congestion effects), PEVs actually consume relatively *less* energy than their ICEV counterparts. The energy consumption model used in this project was based on the data obtained from (29) describing the energy use of a Tesla electric vehicle in terms of ancillary, tires, aerodynamics, and drivetrain. Figure 1b shows the approximated points and the polynomial regression curve fitted to the data using Matlab. The two functions used for energy consumption for ICEVs and PEVs respectively are shown in Table I. The average speed on each link is then multiplied by the length of the link to calculate the energy consumption of the vehicle on that individual link. The total energy consumption is found by aggregating over all vehicles and links in the network. Also in Table I are the adjusted R squared values for both regression models. Values near one indicate that these curves are a reasonably good fit to the data.

**TABLE 1 Energy consumption functions for ICEVs and PEVs**

Energy Consumption (TEC) [kWh/mi]	Adjusted R <sup>2</sup> Value
$EC_{ICEV}(s) = 14.58s^{-0.6253}$	0.9846
$EC_{PEV}(s) = 1.79e-8s^4 - 4.073e-6s^3 + 3.654e-4s^2 - 0.0109s + 0.2372$	0.9651

While the curves in Figure 1 capture the fundamental differences between vehicle technologies, the scale between the two models is significantly different; this data implies that PEVs are about ten times more efficient than ICEVs, which is not accurate. However, for the purposes of this work, it is the difference between the behavior of these two curves that is important. Additionally, these models compare an “average” ICEV with a highly efficient PEV. Finally, these models reflect mobile vehicle energy use only; they do not account for the upstream energy use in terms of the production or transmission of electricity, refining petroleum or transporting products, or other inefficiencies in either process. As technology advances, the energy consumption of both ICEVs and PEVs will likely decrease, particularly in the long-term future period this work is interested in. However, the different efficiency curves will remain a vital factor.

## 5. COMPUTATIONAL RESULTS

This section presents the computational results to the NDP model defined in Section 3. Numerical analysis is provided for the Nguyen–Dupius network. This analysis considers two objective functions, minimizing TSEC and minimizing TSTT. Results are presented for each, and the tradeoff between energy consumption and travel time in regards to network design decisions are discussed. In order to isolate the impact of PEV energy consumption, the computation assumed 100% PEV presence  $\{z_{rs} = 1.0 \ \forall r \in R, \forall s \in S\}$ , unless explicitly stated otherwise.

### 5.1 Nguyen-Dupius Network

The Nguyen-Dupius network (Figure 2) is a small test network consisting of 13 nodes, 19 links, and 4 OD pairs. There are two origins (1 and 4) and two destinations (2 and 3), with a demand between OD pair (1,2) of 1,528, (1,3) of 1,840, (4,2) of 1,680, and (4,3) of 1,360. All links have an initial capacity of 2,200 vehicles per hour (vph) except links 3, 4, 6, and 7 which have a capacity of 1,800, all links have a free flow speed of 50 mph, and BPR design parameters,  $\alpha$  and  $\beta$ , of 0.15 and 4, respectively.

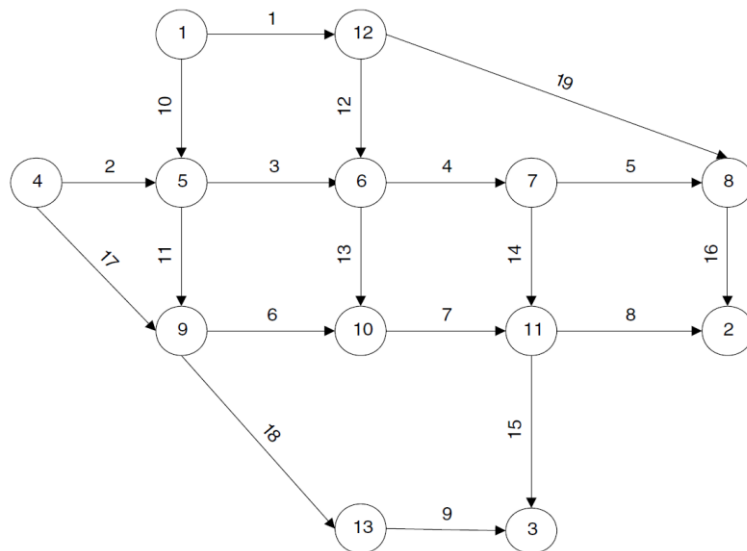


FIGURE 2 The Nguyen-Dupius test network

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The problem is defined as follows: the network planner desires to improve network performance (i.e., TSEC, TSTT, both) by increasing the capacity on individual links. Different design scenarios were explored, defined by the number of links that could be improved, and the amount of capacity to be added. Combinations evaluated include capacity enhancements of 500, 1000, 1500 and 2000 vph, for either 2, 3, 4 or 5 links, for a total of 16 scenarios. The NDP, that is identifying the optimal links to improve, for each of these scenarios was solved using the GA to minimize either TSTT or TSEC for a total of 32 different cases. A large population size of 100, crossover probability of 0.9, and mutation probability of 0.01 were utilized as the GA inputs. Note that the GA was run for a large number of generations (about 500) to allow the GA time to "evolve" to the best solution.

For each case the performance measure is the percentage improvement in TSEC or TSTT (dependent on the specified objective) relative to the base case. This is equal to the percentage decrease in travel time or energy consumption after adding capacity. The base case is defined as the network performance prior to any link improvements.

Table 2 illustrates the results of each experiment for the Nguyen–Dupius network. The number of allowed link improvements is listed on the far left. For each evaluated number of link improvements the specified objective function, capacity allotment per link, performance measure, and set of links identified for expansion for the given scenario are provided from left to right along a row. The total capacity added to the network in each case is the capacity enhancement per link times the number of link improvements allowed. For a given scenario the set of links identified for expansion are highlighted with an ‘X’ in the column. Note that links 2, 3, 13, 18, and 19 were not identified as optimal locations for improvement in any scenario and therefore are included in the table. The presentation style provides a means to compare results by objective and scenario relatively easily. As illustrated, the results reinforce the complex behavior of the NDP, as well as the expected sensitivity to the specified objective function.

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**TABLE 2 Results for discrete design scenario selection on Nguyen-Dupius network**

	Capacity Enhancement per lane	% Performance Measure Improvement	Link Number																
			1	4	5	6	7	8	9	10	11	12	14	15	16	17			
2 Links Improved	TSTT	500 3.6%	X								X								
		1000 9.4%										X	X						
		1500 12.0%										X	X						
		2000 13.5%										X	X						
	TSEC	500 4.2%					X						X						
		1000 3.5%					X					X							
		1500 3.0%			X		X												
		2000 2.7%			X		X												
3 Links Improved	TSTT	500 7.6%									X	X	X						
		1000 12.3%									X	X			X				
		1500 15.3%									X	X			X				
		2000 18.2%	X								X	X							
	TSEC	500 5.3%			X		X						X						
		1000 5.2%	X		X		X												
		1500 4.7%	X		X		X												
		2000 3.7%	X				X					X							
4 Links Improved	TSTT	500 9.7%									X	X	X		X				
		1000 12.6%				X						X	X		X				
		1500 18.2%	X									X	X		X				
		2000 21.7%	X									X	X		X				
	TSEC	500 7.0%	X		X		X						X						
		1000 8.1%	X		X		X					X							
		1500 5.2%	X		X		X					X							
		2000 3.7%	X				X			X		X							
5 Links Improved	TSTT	500 10.2%					X				X	X	X		X				
		1000 15.3%					X				X	X	X		X				
		1500 19.9%	X				X					X	X		X				
		2000 23.4%	X	X								X	X		X				
	TSEC	500 8.5%	X		X		X		X				X						
		1000 8.1%	X		X		X					X		X					
		1500 5.2%	X		X		X					X				X			
		2000 3.7%	X				X	X		X		X							

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For discussion purposes, focus will be on the two performance measures of interest in this research, TSTT and TSEC. When fewer, smaller total improvements were desired (which in some cases may be the more economical option), the two objectives almost always chose different links to improve. This indicates that TSTT and TSEC do not have a positive correlation, i.e., minimizing one objective will not necessarily result in improved network performance for the opposing objective. This implication is further analyzed, and the conflicting behavior is confirmed in Figure 3.

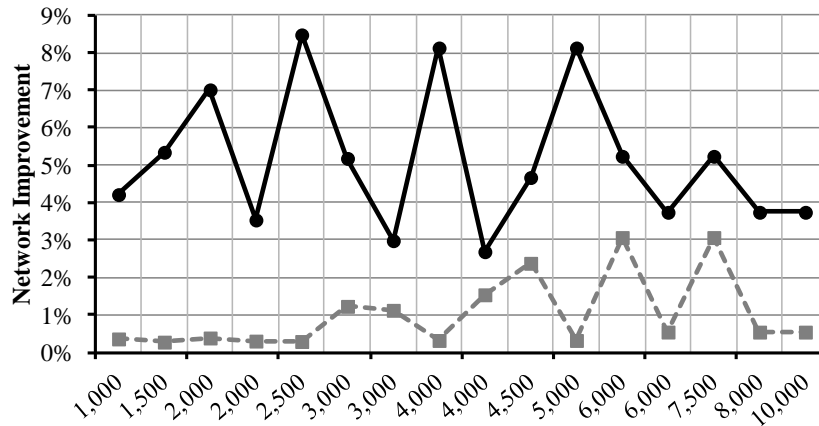
Figure 3 displays the same results that were included in Table 2, with the addition of the corresponding change in the opposite performance measure, where each point is one of the design scenarios presented in Table 2. Figure (3a) shows the results from the design scenarios based on minimizing TSEC and Figure (3b) shows the results for scenarios based on minimizing TSTT. In a number of potential improvement scenarios, the performance measure that was not considered in the optimization problem actually demonstrates *poorer* performance than in the base case. This behavior is more prevalent when the objective of the

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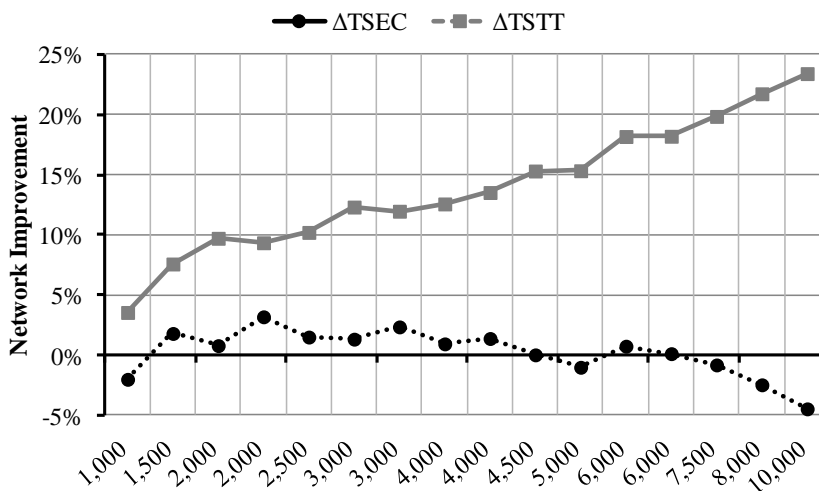
401 NDP is to minimize TSTT, especially in the scenarios that added a greater amount of  
402 capacity. It is therefore likely the selected set of link improvements that minimize TSTT will  
403 actually result in an increase in TSEC. This outcome can be explained by the energy  
404 consumption curves provided in Figure 1. In terms of energy consumption, PEVs are more  
405 efficient at lower speeds than ICEVs. Under this assumption a congested network, which  
406 results in slower speeds on average, will actually result in lower energy consumption than an  
407 uncongested network with a high penetration of PEVs. Because capacity expansion projects  
408 often reduce congestion on a link, therefore reducing travel times, the solution which  
409 minimizes TSTT can be expected to potentially increase TSEC. In addition, because of the  
410 different functional form of PEVs as compared to traditional ICEVs, this conflicting  
411 behaviour may not appear in networks comprised totally of traditional vehicles. However the  
412 observed the negative correlation does not always hold true when the NDP objective is to  
413 minimize TSEC. Under the TSEC objective, multiple scenarios resulted in an optimal  
414 solution that improved both TSTT and TSEC, although the TSTT performance measure  
415 improvement was significantly less than when TSTT was directly minimized.

416 When the objective was to minimize TSEC, multiple scenarios resulted in the same  
417 performance measure, even though additional capacity was added. For example, when 2000  
418 vph were added to 3, 4, or 5 links, 3.7% improvement in TSEC resulted in each case. The  
419 same behavior was observed for an additional capacity of 1000 vph to either 4 or 5 links,  
420 which actually resulted in a 8.1% improvement in TSEC. This is because after adding three  
421 links to the network, improving another link will result in a suboptimal solution, and so the  
422 GA arbitrarily chose a link that did not impact the final system performance. This indicates  
423 that performing additional projects will not necessarily be beneficial for TSEC, whereas  
424 additional projects always provide an improvement in TSTT. Moreover, these results  
425 highlight another contribution of this work, a means for quantitatively evaluating and ranking  
426 potential design projects. Such a ranking will help identify the most cost effective options for  
427 achieving a given objective.

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(a) Total capacity added in design strategy minimizing TSEC



(b) Total capacity added in design strategy minimizing TSTT

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**FIGURE 3 (a) Performance measures for design scenarios minimizing TSEC and (b) performance measures for design scenarios minimizing TSTT**

Furthermore, this work employs a modified multi-objective version of the NSGA II to explore potential tradeoffs between TSTT and TSEC. One of the benefits of a multi-objective GA is its ability to find many Pareto-optimal solutions in a single run, and this diversity of solutions confirmed the findings from computations using a single-objective. Alternative options for two cases can be seen in Figure 3(b), adding 1,500 to 4 links or 2,000 to 4 links, and these results are presented in Table 3. When minimizing solely the objective of TSTT, these cases resulted in poor network performance or even an overall increase for TSEC. When these scenarios were optimized considering both TSEC and TSTT, the GA identified multiple options that improved TSEC as well as TSTT. However, there is a clear trade-off between the behavior of the two opposing objectives. Table 3 displays two options for each scenario, one option favoring TSTT and one option favoring TSEC. These results support the conclusion that one objective does not need to be optimized at the expense of another. Solutions that are beneficial for TSEC and TSTT exist.

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**TABLE 3 Results for multi-objective design scenarios**

# Links Improved	Capacity added per link	$\Delta$ TSTT	$\Delta$ TSEC
4	1500	5.7%	4.0%
4	1500	14.8%	3.1%
4	2000	13.6%	1.5%
4	2000	5.1%	2.9%

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## 6. CONCLUSION

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Finally, design solutions were tested on a network made up of varying levels of PEVs. For a network comprised of 100% ICEVs, it was observed that TSTT and TSEC behave in a similar manner. Minimizing one objective will also result in favorable performance from the other, and when a multi-objective GA is implemented, there are cases that find the same solution as the single-objective variation. This behavior is predictable based on the similarity between the functional form of the ICEV energy consumption curve (Figure 1.a) and the BPR cost function. These findings highlight the fundamental differences between a traditional network comprised of ICEVs and a network of the future that could potentially contain a significant proportion of PEVs.

In this work the network design problem (NDP) is implemented to minimize both TSEC and TSTT, independently and as a multi-objective. The problem was modeled using a bi-level formulation where the upper level was solved using a genetic algorithm and the lower level was a multiclass user equilibrium traffic assignment model. Vehicle energy consumption was computed based on industry data for PEVs and ICEVs. A number of discrete design scenarios were examined, and the results revealed the two performance measures to often be conflicting objectives.

Specifically, when the NDP objective was to minimize only TSTT (the traditional planning objective), the solution often resulted in an increased TSEC relative to the base case. Similarly, when the objective was to minimize only TSEC multiple solutions resulted in an increased TSTT, however there were also solutions which improved both performance measures, especially for higher capacity scenarios. These results motivated the need for considering a multi-objective NDP, which was implemented and identified solutions that improved both TSEC and TSTT. In particular, this works highlights the following findings:

- If multiple objectives are not explicitly considered, it is possible that a design decision intended to improve the network performance of one objective (i.e., TSTT) will do so at the expense of another (i.e., TSEC).
- Design strategies that result in a superior performance for both TSEC and TSTT exist. A multi-objective NDP identifies these potential options.
- PEV energy consumption behaves in a fundamentally different manner from the energy consumption of traditional vehicles and must be explicitly accounted for by network planners.

As PEVs become more prominent, transport network planners will require new research tools that account for the impact of this novel technology. Planned future research will address demand and capacity uncertainty, as well as incorporating dynamic traffic assignment into the sub-problem. These extensions will provide a more accurate appraisal of energy consumption, particularly by accounting for the dynamics of vehicle flow and energy use. Additionally, forthcoming data on the expected penetration rates of PEVs by region can

489 be incorporated into the model to quantify the spatiotemporal energy demands generated for a  
 490 realistic mix of PEVs and ICEVs, an essential component for regional energy providers.

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#### 495 **REFERENCES**

- 496 (1) Perujo, A., and B. Ciuffo, The introduction of electric vehicles in the private fleet:  
 497 Potential impact on the electric supply system and on the environment. A case study for  
 498 the Province of Milan, Italy. *Energy Policy*, Vol. 38, No. 8, 2010, pp. 4549-4561.
- 499 (2) Clement-Nyns, K., E. Haesen, and J. Driesen. The Impact of Charging Plug-In Hybrid  
 500 Electric Vehicles on a Residential Distribution Grid. *Power Systems, IEEE*  
 501 *Transactions on* , Vol. 25, No.1, 2010, pp.371-380.
- 502 (3) Yang, H. and M.G.H. Bell H. Models and algorithms for road network design: a review  
 503 and some new developments. *Transport Reviews*, Vol.18, No. 3, 1997, pp. 257-278.
- 504 (4) LeBlanc, L. An algorithm for the discrete network design problem. *Transportation*  
 505 *Science*, Vol. 9, 1975, pp. 183–199.
- 506 (5) Dantzig, G. B., R.P. Harvey, Z.F. Landsowne, D.W. Robinson, and S.F. Maier. (1979),  
 507 Formulating and solving the network design problem by decomposition. *Transportation*  
 508 *Research*, Vol. 13B, 1979, pp 5–17.
- 509 (6) Boyce, D. E. and B.N. Janson. A discrete transportation network design problem with  
 510 combined trip distribution and assignment. *Transportation Research*, Vol. 14B, 1980,  
 511 pp 147–154.
- 512 (7) Chen, M. and A.S. Alfa. A Network Design Algorithm Using a Stochastic Incremental  
 513 Traffic Assignment Approach. *Transportation Science*, Vol 25, 1991, 215–224.
- 514 (8) Davis, G. A. Exact local solution of the continuous network design problem via  
 515 stochastic user equilibrium assignment, *Transportation Research*, Vol. 28B, 1994, pp.  
 516 61–75.
- 517 (9) Magnanti, T. L. and R.T. Wong, R. T. Network design and transportation planning:  
 518 models and algorithms. *Transportation Science*, Vol. 18, 1984, pp. 1–55.
- 519 (10) Friesz, Terry L. et al. The multiobjective equilibrium network design problem revisited:  
 520 A simulated annealing approach. *European Journal of Operational Research*, Vol. 65,  
 521 No.1, 1993, pp. 44-57.
- 522 (11) Teng J Y, and G.H. Tzeng. A multiobjective programming approach for selecting non-  
 523 independent transportation investment alternatives. *Transportation Research Part B*,  
 524 Vol 30, 1996, pp. 291 – 307,
- 525 (12) Sun, D. R.F. Benekohal, and S.T. Waller. Multiobjective traffic signal timing  
 526 optimization using non-dominated sorting genetic algorithm. *Intelligent Vehicles*  
 527 *Symposium, 2003. Proceedings. IEEE* , Vol. 198, No. 203, 2003, pp. 9-11.
- 528 (13) Ukkusuri, S., T.V. Mathew, and S.T. Waller. Robust Network Design Problem Under  
 529 Demand Uncertainty. *Computer-Aided Civil and Infrastructure Engineering*, Vol. 22,  
 530 2007, pp. 6-18.
- 531 (14) Gardner, L., A. Unnikrishnan, and S.T. Waller. Robust Pricing of Transportation  
 532 Network Under Uncertain Demand. In *Transportation Research Record: Journal of the*  
 533 *Transportation Research Board*, No. 2085, Transportation Research Board of the  
 534 National Academies, Washington, D.C. 2008, pp. 21-30.
- 535 (15) Duthie, J. and S.T. Waller, Incorporating Environmental Justice Measures into  
 536 Equilibrium-Based Network Design. In *Transportation Research Record: Journal of*

- 537 *the Transportation Research Board*, No. 2089, Transportation Research Board of the  
538 National Academies, Washington, D.C. 2008, pp. 58-65.
- 539 (16) Sharma, S., and T.V. Mathew. Multiobjective network design for emission and travel-  
540 time trade-off for a sustainable large urban transportation network. *Environment and*  
541 *Planning B: Planning and Design*, Vol. 38, No. 3, 2011, pp. 520–538.
- 542 (17) Ferguson, E. M., J. Duthie, and S.T. Waller. Comparing Delay Minimization and  
543 Emissions Minimization in the Network Design Problem. *Computer-Aided Civil and*  
544 *Infrastructure Engineering*, Vol. 27, No. 4, 2012, pp. 288-302.
- 545 (18) Artmeier, A., J. Haselmayr, M. Leucker, and M. Sachenbacher. The Shortest Path  
546 Problem Revisited: Optimal Routing for Electric Vehicles. *KI 2010 Advances in*  
547 *Artificial Intelligence*, No. 6359, 2010, pp. 309-316.
- 548 (19) Jiang, N., C. Xi. and S.T. Waller. Path-Constrained Traffic Assignment: Model and  
549 Algorithm. Presented at the 91st Annual Meeting of the Transportation Research Board,  
550 Transportation Research Board of the National Academies, Washington, D.C., 2012.
- 551 (20) Gardner, L., M. Duell, S.T. Waller, and I. Macgill. The System Impact of Travel  
552 Demand Variability in the Context of Electric Vehicles. Hawaii International  
553 Conference on Systems Sciences, 2012.
- 554 (21) Sheffi, Y. *Urban Transportation Networks: Equilibrium Analysis with Mathematical*  
555 *Programming Methods*, Englewood Cliffs, NJ, USA, 1985, Prentice-Hall.
- 556 (22) Karoonsoontawong, A. and S.T. Waller. Dynamic Continuous Network Design  
557 Problem: Linear Bilevel Programming and Metaheuristic Approaches. In  
558 *Transportation Research Record: Journal of the Transportation Research Board*,  
559 Transportation Research Board of the National Academies, Washington, D.C., 2006.  
560 No. 1964, pp. 104-117.
- 561 (23) Deb, K., A. Pratap, S. Agarwal, and T. Meyarivan. A fast and elitist multiobjective  
562 genetic algorithm: NSGA-II. *Evolutionary Computation, IEEE Transactions*, Vol. 6,  
563 No.2, 2002, pp.182-197.
- 564 (24) Wardrop, J.G. Some Theoretical Aspects of Road Traffic Research. *Proceedings,*  
565 *Institution of Civil Engineers*, Vol II, No. 1, 1952, pp. 325-378.
- 566 (25) Joumard, R., M. André, R. Vidon, P. Tassel, and Pruvost, C. Influence of driving  
567 cycles on unit emissions from passenger cars. *Atmospheric Environment*, Vol. 34, No.  
568 27, 2000, pp. 4621–4630.
- 569 (26) Graver, B. M., H.C., Frey, and H. W. Choi, H. In-Use Measurement of Activity, Energy  
570 Use, and Emissions of a Plug-in Hybrid Electric Vehicle. *Environmental Science &*  
571 *Technology*, Vol. 45, No. 20, 2011, pp. 9044-9051.
- 572 (27) Ford, J., G. Khowailed, J. Blackburn, and K. Sikes. A Comparative Study on Emerging  
573 Electric Vehicle Technology Assessments, 2011, Retrieved from  
574 <http://www.osti.gov/bridge/servlets/purl/1008834-DQbYtD/>
- 575 (28) US Environmental Protection Agency. *Motor Vehicle Emission Simulator. MOVES*  
576 *2010 user guide*". EPA report EPA-420-B-09-041, Office of Transportation and Air  
577 Quality, December 2009.
- 578 (29) Tesla Motors. Energy Efficiency of Electric Vehicles. Accessed 17-June-2012 from  
579 <http://www.teslamotors.com/goelectric/efficiency>